A STUDY OF SINGLE TRANSMIT ANTENNA SELECTION WITH MODULATION

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Abstract: Multiple-input multiple-output (MIMO) systems have attracted a vast amount of interest, due to improvements offered in capacity and diversity. However, several challenges still remain. Single transmit antenna selection with modulation (STASM) is an important closed-loop variant of MIMO, and addresses several of its challenges, while achieving full-diversity. On this note, the average symbol error probability (ASEP) of STASM with M-ary quadrature amplitude modulation (M-QAM) and M-ary phase shift keying (M-PSK) is formulated and validates the Monte Carlo simulation results. The formulated ASEP expressions are relatively easy to evaluate. Euclidean distance-based antenna selection for spatial modulation (EDAS-SM) is an innovative closed-loop MIMO scheme that provides many advantages. However, since STASM achieves a full-diversity compared to EDAS-SM, there exists a cross-over point after which its error performance is superior to the latter. For multiple receive antennas, the cross-over point only occurs in the moderate-to-high signal-to-noise ratio region, which may be difficult to achieve in practice. Hence, an adaptive transmit mode switching system based on STASM and EDAS-SM as transmission candidates is proposed. A selection criterion for the transmission candidate is based on minimizing the instantaneous symbol error probability in every transmission interval. By switching between STASM and EDAS-SM, the proposed scheme minimizes the ASEP.

Keywords: Adaptive multiple-input multiple-output, Euclidean distance-based antenna selection for spatial modulation, single transmit antenna selection with modulation.

1. INTRODUCTION

In recent times, there is a ubiquitous demand for improved data rates and reliable transmission due to the success of cellular services, multimedia applications and the internet. In this regard, multiple-input multiple-output (MIMO) systems have gained much interest due to its potential for improvements in terms of capacity, diversity and smart antenna usage. However, there are several challenges that need to be addressed. For example, some of the well-known challenges are inter-channel interference (ICI) at the receiver, the requirement for inter-antenna synchronization (IAS) at the transmitter and multiple radio frequency (RF) chains, increased hardware and computational complexity. On this note, spatial modulation (SM) has been proposed by Mesleh et al. [1, 2] to alleviate these challenges. The key idea of SM is to map information to the index of a transmit antenna element. The corresponding antenna is then activated to transmit a symbol from an amplitude and/or phase modulation (APM) constellation set. This technique has inherent advantages. For example, IAS at the transmitter is not required; there is no ICI at the receiver; furthermore, only a single RF chain is required, consequently also improving energy efficiency. its introduction, a vast amount of research into SM has been performed in the research community. This has been primarily three-pronged: improvement of reliability, throughput and decreased system complexity [3, 4].

A key disadvantage of SM is that its potential for transmit diversity is not exploited. On this note, several closed-loop

schemes for SM have been investigated [3]. In general, the closed-loop schemes of SM are based on: adaptive modulation, transmit precoding, antenna selection and combinations thereof [3].

Of particular interest, antenna selection for SM was investigated in [5, 6]. In [5, 6], Yang et al. presented three closed-loop transmit mode switching schemes for SM, viz. adaptive SM (ASM), optimal-hybrid SM (OH-SM) and concatenated SM (C-SM). The ASM scheme [5] selects the optimum modulation candidate among several predetermined candidates by maximizing the minimum Euclidean distance (MED) between transmission vectors. The transmitter then employs the selected candidate in the subsequent frame. The OH-SM and C-SM schemes [6] employ the same basic idea; however, in OH-SM, the candidate modes additionally make use of transmit antenna selection. While OH-SM yields superior error performance among these schemes, all impose a relatively high computational complexity (CC). Motivated to reduce the high CC of these schemes, the authors of [7, 8], investigated Euclidean distance-based antenna selection for SM (EDAS-SM). Given N_T transmit antennas, the EDAS-SM scheme searches all possible enumerations of N_{SM} transmit antennas, where 1 < N_{SM} < N_T , for the enumeration that maximizes the MED between transmission vectors. Substantial improvement in error performance was demonstrated at a significantly lower CC [7]. In [8], by exploiting mirror symmetry, further modifications to EDAS-SM decreased the imposed CC. The CC was reduced even further by

Wang *et al.* [9] by exploiting rotational symmetry. Ntontin *et al.* [10] presented a suboptimal approach for EDAS-SM by invoking singular value decomposition and the Rayleigh-Ritz theorem, which renders the CC independent of the constellation size.

Meanwhile, another well-known closed-loop MIMO technique, single transmit antenna selection with modulation (STASM) [11-13], exhibits similar advantages to SM. For example, STASM also employs a single active transmit antenna, hence IAS is not required, zero ICI is achieved and a single RF chain is required. Improvements over SM due to the closed-loop strategy, are the full-diversity order, that can be achieved asymptotically [11-13], and zero antenna detection error.

In the literature, the investigation of EDAS-SM has not included benchmarking against STASM.

Motivated by the above, the contributions of this paper are as follows: a. The average symbol error probability (ASEP) of STASM with M-ary quadrature amplitude modulation (M-QAM) and M-ary phase shift keying (M-PSK) is formulated, b. Motivated by a comparison between STASM and EDAS-SM, an adaptive transmit mode switching system based on STASM and EDAS-SM as the possible transmission candidates is investigated. The instantaneous symbol error probability (ISEP) is employed as a selection criterion for the transmission candidate.

The structure of the remainder of this paper is as follows: In Section 2, the background for EDAS-SM and STASM is presented. The formulation of ASEP for STASM with M-QAM and M-PSK is presented in Section 3. Section 4 includes a comparison of the error performance of STASM and EDAS-SM, which forms a motivation for the resulting proposed adaptive system based on transmit mode switching between STASM and EDAS-SM. Finally, conclusions are drawn in Section 5.

2. BACKGROUND

2.1 EDAS-SM

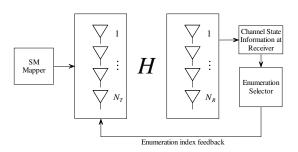


Figure 1: System model of EDAS-SM [7].

The system model of EDAS-SM is illustrated in Figure 1, which assumes a MIMO configuration with N_T transmit antennas, N_R receive antennas and a perfect feedback link to the transmitter.

Given N_T transmit antennas, antenna selection is employed, such as to select an enumeration of N_{SM} antennas, where $1 < N_{SM} < N_T$. The mechanism for antenna selection is discussed shortly. An SM mapper [1, 2] is then employed prior to transmission of the message. The received signal of EDAS-SM is defined as [7, 8]:

$$y = \sqrt{\gamma} H_{SM} x + \eta \tag{1}$$

where γ is the average signal-to-noise ratio (SNR) at each receive antenna, $m{H}_{SM} = \begin{bmatrix} m{h}_1 & m{h}_2 & \cdots & m{h}_{N_{SM}} \end{bmatrix}$ is an $N_R \times N_{SM}$ sub-matrix of an $N_R \times N_T$ matrix $\vec{\boldsymbol{H}}$ with $1 < N_{SM} < N_T$, and its entries are independent and identically distributed (i.i.d.) complex Gaussian random variables with zero mean and unit variance. The transmit symbol is given by $x = e_k s_q$, where $e_k, k \in [1:N_{SM}]$, is an $N_{SM} \times 1$ vector with a single non-zero element a = 1located at the k-th position and k represents a transmit antenna index, chosen by mapping $\log_2 N_{SM}$ message bits to the chosen N_{SM} antenna indices. The antenna k is then activated to transmit an M-QAM or M-PSK symbol s_q , $q \in [1:M]$, where $E\{|s_q|^2\} = 1$ is assumed. η represents the presence of additive white Gaussian noise (AWGN) and its entries are i.i.d. complex Gaussian random variables with zero mean and unit variance.

Assuming channel state information at the receiver (CSIR), the optimal detector for EDAS-SM employs the maximum-likelihood (ML) rule and is given as [7, 8]:

$$[\hat{k}, s_{\hat{q}}] = \underset{s_q \in \mathbf{\chi}, k \in [1:N_{SM}]}{\operatorname{argmin}} \|\mathbf{y} - \sqrt{\gamma} \mathbf{h}_k s_q\|_F^2 \qquad (2)$$

where χ is the set of all possible s_a .

In [5, 6], the authors approximate the average bit error probability of EDAS-SM by considering the nearest neighbour approximation of the pairwise error probability (PEP), defined by [5, 6],

$$P_b \approx \lambda \cdot Q\left(\sqrt{\frac{\gamma}{4} \cdot \min_{\boldsymbol{x}_1 \neq \boldsymbol{x}_2 \in \boldsymbol{\chi}_1} \|\boldsymbol{H}_{SM}(\boldsymbol{x}_1 - \boldsymbol{x}_2)\|_F^2}\right)$$
(3)

$$= \lambda \cdot Q\left(\sqrt{\frac{\gamma}{4} \cdot d_{min}^2(\boldsymbol{H}_{SM})}\right) \tag{4}$$

where λ represents the number of neighbourhood points, x_1 and x_2 are the transmitted and detected symbol vectors, respectively. The set of all possible transmit symbol vector combinations of x_1 and x_2 are contained in χ_1 and x_n , $n \in [1:2]$, is denoted by $e_k s_q$ and $d_{min}(\boldsymbol{H}_{SM})$ is the MED between the vectors.

From (4), it is evident that the argument of the Q-function should be maximized to minimize the PEP. Hence, in [5, 6], in order to select the optimal candidate enumeration of N_{SM} transmit antennas when N_T transmit antennas are employed, the following Euclidean distance-based decision metric is solved, such as to minimize error probability [5,

6],

$$\ell_{selected} = \underset{\ell=1:N}{\operatorname{argmax}} \left(\min_{\boldsymbol{x}_1 \neq \boldsymbol{x}_2 \in \boldsymbol{\chi}_1} \left\| \boldsymbol{H}_{SM} \left(\boldsymbol{x}_1 - \boldsymbol{x}_2 \right) \right\|_F^2 \right)$$
(5)

where the columns of \boldsymbol{H}_{SM} correspond to the elements of the ℓ^{th} enumeration of a set of $N=\binom{N_T}{N_{SM}}$ possible transmit antenna enumerations.

The computational complexity of (5) was formulated as $O(NN_T^2M^2)$ [7] and is significantly high, limiting the practicality of the method. In the interest of practical realization of (5), [7] demonstrated the equivalence between (5) and the quantity $\ell_{selected} = \arg\max_{\ell=1:N} (\min \boldsymbol{D}(\ell))$, where $\boldsymbol{D}(\ell)$ is an $N_{SM} \times N_{SM}$ sub-matrix of an upper triangular $N_T \times N_T$ matrix \boldsymbol{D} obtained by deleting the rows and columns that are absent in ℓ . Note, the elements of \boldsymbol{D} are real.

For M-QAM, the (i, j)-th element of \boldsymbol{D} is computed as follows [7]:

$$D_{i,j} = \begin{cases} \left(d_{min}^{QAM}\right)^{2} \|\mathbf{h}_{i}\|_{F}^{2}, & i = j\\ \min_{\substack{s_{1I}, s_{2I} \in \mathbf{M}_{1}\\ s_{1Q}, s_{2Q} \in \mathbf{M}_{2}}} \|\mathbf{R}_{\mathbf{s}}\|_{F}^{2}, & i \neq j \end{cases}$$
(6)

where the minimum distance between any two QAM symbols is given as $d_{min}^{QAM} = 2$ and

$$\mathbf{R_s} \ = \ \mathbf{R} \begin{bmatrix} s_{1I} \\ s_{1Q} \\ -s_{2I} \\ -s_{2Q} \end{bmatrix} = \begin{bmatrix} r_{1,1}s_{1I} - r_{1,3}s_{2I} - r_{1,4}s_{2Q} \\ r_{2,2}s_{1Q} - r_{2,3}s_{2I} - r_{2,4}s_{2Q} \\ -r_{3,3}s_{2I} \\ -r_{4,4}s_{2Q} \end{bmatrix}$$

with ${\bf R}$ a 4 \times 4 upper-triangular matrix with zero entries at the locations (1,2) and (3,4) resulting from the QR decomposition of the channel matrix [7]. ${\bf R_s}$ is computed for pulse amplitude modulation (PAM) constellation points $s_{1I}, s_{2I} \in M_1$ and $s_{1Q}, s_{2Q} \in M_2$ for separable QAM signal sets (if an M-QAM signal set can be equivalently written as the Cartesian product of a \sqrt{M} -PAM constellation set with itself then the QAM signal set is known as separable). Note, M_1 and M_2 represent one half of the in-phase and quadrature PAM constellation sets, respectively, due to rotational symmetry [9].

Note, in this paper, only EDAS-SM for M-QAM is considered; however, EDAS-SM for M-PSK is also realized using (5), where only one constellation point is required in the search, due to rotational symmetry [9].

2.2 STASM

Consider a MIMO system with N_T transmit antennas, N_R receive antennas and a perfect feedback link to the transmitter. The STASM scheme assumes a system model as illustrated in Figure 2.

The $N_R \times 1$ received signal vector can be defined as [13],

$$y = \sqrt{\gamma} H x + \eta \tag{7}$$

where γ is the average SNR at each receive antenna, \boldsymbol{H} is the $N_R \times N_T$ channel gain matrix defined as $\boldsymbol{H} = \begin{bmatrix} \boldsymbol{h}_1 & \boldsymbol{h}_2 & \cdots & \boldsymbol{h}_{N_T} \end{bmatrix}$, where \boldsymbol{h}_j ,

 $j \in [1:N_T]$, is the j-th column of \boldsymbol{H} , defined as $\boldsymbol{h}_j = \begin{bmatrix} h_{1,j} & h_{2,j} & \cdots & h_{N_R,j} \end{bmatrix}^T$. The elements of \boldsymbol{H} are assumed to be i.i.d. complex Gaussian random variables with zero mean and unit variance. \boldsymbol{x} is an $N_T \times 1$ transmit vector of the form $\boldsymbol{e}_j s_q$, where \boldsymbol{e}_j , $j \in [1:N_T]$ is an $N_T \times 1$ vector with one non-zero unit entry in the j-th position and s_q , $q \in [1:M]$ is a complex symbol drawn from an M-QAM or M-PSK set. We assume $E\{|s_q|^2\}=1$. The $N_R \times 1$ noise vector $\boldsymbol{\eta}$ is a complex AWGN vector with i.i.d. elements having zero mean and unit variance. Assuming CSIR, a single transmit antenna is selected based on the largest column \hat{j} of the channel matrix, such that $\|\boldsymbol{h}_{\hat{j}}\|_F > \|\boldsymbol{h}_{j}\|_F$, $j \in [1:N_T]$, $\hat{j} \neq j$. The index, \hat{j} of the selected antenna is then fed back to the transmitter, which transmits s_q from antenna \hat{j} , hence \boldsymbol{e}_j above is denoted $\boldsymbol{e}_{\hat{j}}$.

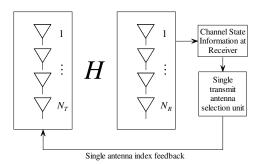


Figure 2: System model of STASM [11-13].

Optimal detection using the ML rule is assumed and is defined as,

$$s_{\hat{q}} = \operatorname*{argmin}_{s_q \in \mathbf{\chi}} \| \mathbf{y} - \sqrt{\gamma} \mathbf{h}_{\hat{j}} s_q \|_F^2$$
 (8)

3. PERFORMANCE ANALYSIS OF STASM

In [11-13], the theoretical average error probability of STASM for binary phase-shift keying was presented. From searching the open literature, the authors did not come across an extension of the analysis to the case of M-QAM and M-PSK for arbitrary N_T and N_R . In this section, we extend the analysis to M-QAM and M-PSK with arbitrary N_T and N_R for a frequency-flat Rayleigh fading channel. The resulting analysis is relatively easy to evaluate and results in a tight match with simulation results.

3.1 ASEP of STASM with M-QAM

For M-QAM, the ASEP assuming only AWGN is given as [14, (45)]:

$$P_M(\gamma) = 4\varphi - 4\varphi^2 \tag{9}$$

where
$$\varphi = \left(1 - \frac{1}{\sqrt{M}}\right) Q\left(\sqrt{\frac{3\gamma}{M-1}}\right)$$
.

For STASM, the probability density function (PDF) of the instantaneous receive SNR, $\gamma_s = \gamma \sum_{r=1}^{N_R} |h_{\hat{j},r}|^2$, for a frequency-flat Rayleigh fading channel is defined as

$$f_{\gamma_s}\left(\gamma_s\right) = \frac{1}{\gamma} f_{N_T}\left(\frac{\gamma_s}{\gamma}\right)$$
, where

$$f_{N_T}(x) = \frac{N_T}{(N_R - 1)!} \times \left(1 - e^{-x} \sum_{i=0}^{N_R - 1} \frac{x^i}{i!}\right)^{N_T - 1} \frac{x^{N_R - 1}}{e^x} \quad (10)$$

and $x = \frac{\gamma_s}{\gamma}$ [13].

Setting $\alpha=1-\frac{1}{\sqrt{M}},\ \beta=\frac{3}{M-1}$ and employing approximations of the Q-function [14, Section V], the ASEP is formulated as:

$$P_{e} \approx \int_{0}^{\infty} \left(\frac{1}{3} \alpha e^{-0.5\beta \gamma x} + \alpha e^{-\frac{2}{3}\beta \gamma x} - \frac{1}{2} \alpha^{2} e^{-\beta \gamma x} \right) \times \frac{N_{T}}{(N_{R} - 1)!} \left(1 - e^{-x} \sum_{i=0}^{N_{R} - 1} \frac{x^{i}}{i!} \right)^{N_{T} - 1} \times x^{N_{R} - 1} e^{-x} dx \quad (11)$$

The term $(1+X)^{N_T-1}$, represents a binomial expansion [15], assuming $X=-e^{-x}\sum_{i=0}^{N_R-1}\frac{x^i}{i!}$; hence, (11) can be modified to:

$$P_{e} \approx \int_{0}^{\infty} \left(\frac{1}{3} \alpha e^{-0.5\beta \gamma x} + \alpha e^{-\frac{2}{3}\beta \gamma x} - \frac{1}{2} \alpha^{2} e^{-\beta \gamma x} \right) \times \frac{N_{T}}{(N_{R} - 1)!} \sum_{k=0}^{N_{T} - 1} (-1)^{k} e^{-x(k+1)} \binom{N_{T} - 1}{k} \times \binom{\sum_{i=0}^{N_{R} - 1} \frac{x^{i}}{i!}}{i!} x^{N_{R} - 1} dx \quad (12)$$

The term $\left(\sum_{i=0}^{N_R-1} \frac{x^i}{i!}\right)^k$ represents a multinomial expansion [15]. To solve the integral, we employ the following relation [17, 18]:

$$\left(\sum_{i=0}^{N_R-1} \frac{x^i}{i!}\right)^k = \sum_{i=0}^{k(N_R-1)} \beta_{i,k} x^i$$
 (13)

where

$$\beta_{i,k} = \sum_{j=i-N_B+1}^{i} \frac{\beta_{j,k-1}}{(i-j)!} R(j)$$
 (14)

and $\beta_{0,0}=\beta_{0,k}=1,$ $\beta_{i,1}=\frac{1}{i!},$ $\beta_{1,k}=k.$ Note R(j) is a rectangular window defined as:

$$R(j) = \begin{cases} 1 & 0 \le j \le (k-1)(N_R - 1) \\ 0 & otherwise \end{cases}$$
 (15)

Solving the integral in (12), term-by-term, we arrive at:

$$P_{e} \approx \frac{\alpha N_{T}}{(N_{R} - 1)!} \sum_{k=0}^{N_{T} - 1} (-1)^{k} {N_{T} - 1 \choose k} \times \sum_{i=0}^{k(N_{R} - 1)} \beta_{i,k} (i + N_{R} - 1)! \times \left\{ \frac{1}{3} A_{1}^{-(i+N_{R})} + B_{1}^{-(i+N_{R})} - \frac{1}{2} \alpha C_{1}^{-(i+N_{R})} \right\}$$
(16)

where $A_1=\frac{1}{2}\beta\gamma+k+1,\ B_1=\frac{2}{3}\beta\gamma+k+1$ and $C_1=\beta\gamma+k+1.$

3.2 ASEP of STASM with M-PSK

For M-PSK, the ASEP assuming only AWGN is given as [16, (6.16)]:

$$P_M(\gamma) = 2Q\left(\sqrt{2\gamma}\sin\left(\frac{\pi}{M}\right)\right) \tag{17}$$

Accordingly, the ASEP for a frequency-flat Rayleigh fading channel may be formulated as:

$$P_e \approx \int_0^\infty 2Q \left(\sqrt{2\gamma x}\alpha\right) \frac{N_T}{(N_R - 1)!} x^{N_R - 1} e^{-x} \times \left(1 - e^{-x} \sum_{i=0}^{N_R - 1} \frac{x^i}{i!}\right)^{N_T - 1} dx \quad (18)$$

where $\alpha = \sin\left(\frac{\pi}{M}\right)$.

Employing an approximation of the Q-function [14, Section V] and simplifying, as earlier, we arrive at:

$$P_{e} \approx \int_{0}^{\infty} \left\{ \frac{1}{6} e^{-\gamma x \alpha^{2}} + \frac{1}{2} e^{-\frac{4}{3}\gamma x \alpha^{2}} \right\} \times \frac{N_{T}}{(N_{R} - 1)!} \sum_{k=0}^{N_{T} - 1} (-1)^{k} e^{-(k+1)x} \binom{N_{T} - 1}{k} \times \sum_{i=0}^{k(N_{R} - 1)} \beta_{i,k} x^{i+N_{R} - 1} dx \quad (19)$$

Integrating term-by-term, we have:

$$P_{e} \approx \frac{N_{T}}{(N_{R}-1)!} \sum_{k=0}^{N_{T}-1} (-1)^{k} {N_{T}-1 \choose k} \times \sum_{i=0}^{k(N_{R}-1)} \beta_{i,k} (i+N_{R}-1)! \left\{ \frac{1}{6} A_{2}^{-(i+N_{R})} + \frac{4}{6} A_{2}^{-(i+N_{R})} \right\}$$
(20)

where $A_2 = \gamma \alpha^2 + k + 1$.

3.3 Numerical Results

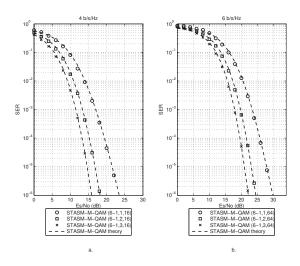


Figure 3: Validation of Monte Carlo simulation results for M-QAM with $N_R = 1, 2$ and 3.

In this subsection, we validate the Monte Carlo simulation results of STASM with M-QAM and M-PSK for $N_R=1,\ 2$ and 3. A frequency-flat Rayleigh fading channel and AWGN is assumed. The notation used to denote the MIMO configuration for STASM is STASM-M-QAM/PSK- $(N_T$ -1, N_R , M). We consider two spectral efficiencies: 4 b/s/Hz and 6 b/s/Hz.

In Figure 3, the results for M-QAM demonstrate a tight match between the Monte Carlo simulation results and the formulated ASEP expression (16). Figure 4 presents the results for M-PSK. Once again, the Monte Carlo simulation results are validated by the formulated ASEP expression (20). A tight match is evident. It is also evident that STASM with M-QAM is superior to STASM with M-PSK; therefore, in the remainder of investigations, we consider M-QAM.

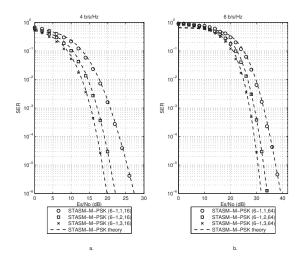


Figure 4: Validation of Monte Carlo simulation results for M-PSK with $N_R=1,\,2$ and 3.

4. PROPOSED ADAPTIVE TRANSMIT MODE SWITCHING WITH STASM AND EDAS-SM

4.1 A Comparison of SM, EDAS-SM and STASM

In this section, we draw comparisons between SM, EDAS-SM and STASM. Since, the M-QAM results for STASM are superior to M-PSK (refer to Figure 3 and 4) we assume M-QAM in the remainder of investigations. Furthermore, a frequency-flat Rayleigh fading channel in the presence of AWGN is assumed. Additionally, CSIR and a perfect feedback link to the transmitter is assumed. The notation used to denote the MIMO configuration employed is as follows: $SM-(N_T,N_R,M)$, EDAS-SM- (N_T-N_{SM},N_R,M) , STASM- (N_T-1,N_R,M) . We first begin by comparing EDAS-SM to SM (this is due to some erroneous results in the literature [8]).

First, we investigate EDAS-SM compared to SM. Simulation results for a spectral efficiency of 4 b/s/Hz are presented in Figure 5 for SM- $(4,N_R,4)$ and EDAS-SM- $(6-4,N_R,4)$ with $N_R=2$ and 3.

It is evident that EDAS-SM yields a significant SNR gain over SM. For example, at a symbol error rate (SER) of 10^{-5} , for $N_R=2$ and $N_R=3$ an SNR gain of approximately 11.25 dB and 7 dB, respectively, is evident. Furthermore, the slope of the SER curves demonstrate the improvement in diversity.

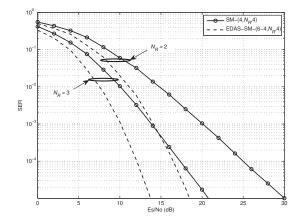


Figure 5: Comparison of SER performance for SM and EDAS-SM for 4 b/s/Hz with $N_R=2$ and 3.

Next, we draw comparisons between STASM and EDAS-SM. For validation purposes, we employ the method used in [19] to generate the SER bound for EDAS-SM, while (16) is employed for STASM. The validation curves for EDAS-SM are generated using the form $c/\gamma^{N_R(N_T-N_{SM}+1)}$ [19], where c is a positive constant determined during simulation (for 4 b/s/Hz, the constant employed for $N_R=1,2,3$ are $c_1=2.36\times 10^4,$ $c_2=1.32\times 10^6$ and $c_3=6.98\times 10^7,$ respectively, while the constants $c_4=1.65\times 10^7,$ $c_5=2.53\times 10^{10}$ and $c_6=4.20\times 10^{13},$ respectively, are employed for 6 b/s/Hz), given that the diversity order of EDAS-SM is $N_R\,(N_T-N_{SM}+1)$ [19]. Validation curves are suitable

reference curves at high SNR [19]; hence, we present results down to an SER of 10^{-8} .

In the first investigation, we consider a spectral efficiency of 4 b/s/Hz.

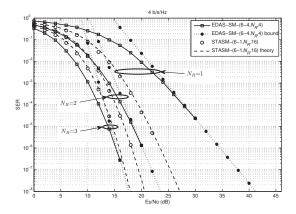


Figure 6: Comparison of SER performance for STASM and EDAS-SM for different N_R and 4 b/s/Hz.

The SER performance results for EDAS-SM-(6-4, N_R ,4) and STASM-(6-1, N_R ,16) with $N_R=1$, 2 and 3 are presented in Figure 6. For $N_R=1$, at a SER of 10^{-8} , STASM exhibits an SNR gain of approximately 14 dB over EDAS-SM. For $N_R=2$ the SNR gain yielded is approximately 3 dB. For $N_R=3$, EDAS-SM-(6-4,3,4) initially outperforms STASM-(6-1,3,16) but converges with an increase in SNR. This is expanded on later.

In the second test, a spectral efficiency of 6 b/s/Hz was considered and the results generated for EDAS-SM-(6-4, N_R ,16) and STASM-(6-1, N_R ,64) with $N_R = 1$, 2 and 3 are presented in Figure 7.

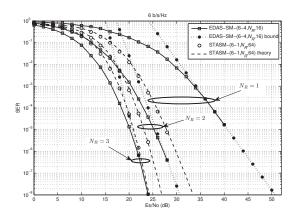


Figure 7: Comparison of SER performance for STASM and EDAS-SM for different N_R and 6 b/s/Hz.

Once again, STASM outperforms EDAS-SM for $N_R \leq 2$. For example, at an SER of 10^{-8} , the SNR gain yielded for $N_R=1$ and $N_R=2$ is 18 dB and 4 dB, respectively. For $N_R=3$, similar behavior as demonstrated in Figure 6 is evident. Returning to the case of $N_R=3$, and once again noting the diversity order of STASM and EDAS-SM

as $d_1 = N_R N_T$ [13] and $d_2 = N_R (N_T - N_{SM} + 1)$ [19], respectively, it is clear that the slope of STASM will always be greater than that of EDAS-SM, since $N_{SM} > 1$. This implies a cross-over point between the SER curves of STASM and EDAS-SM, whenever the latter is superior in the low-to-medium SNR regime. For the case of 4 b/s/Hz and 6 b/s/Hz, in Figure 8, we have extended the range of SNRs plotted to demonstrate the cross-over points between the SER curves of STASM and EDAS-SM. For 4 b/s/Hz, until approximately 19 dB, EDAS-SM is superior; however, beyond the cross-over point, STASM is superior. For 6 b/s/Hz, the same behavior is demonstrated, i.e. STASM begins to outperform EDAS-SM after the cross-over point at approximately 24.8 dB.

The investigations clearly demonstrate that STASM is substantially superior for $N_R = 1$ at low-to-high SNRs. Although STASM achieves full-diversity $(N_T N_R)$ compared to EDAS-SM $(N_R(N_T - N_{SM} + 1))$ the cross-over point for $N_R > 1$ usually occurs in the moderate-to-high SNR region. In the interest of energy efficiency, operation at these SNRs may not be practical, hence EDAS-SM would be the superior choice. Thus, depending on the number of receive antennas employed, EDAS-SM may be superior to STASM for practical SNRs. With reliability in mind, and based on the above comparisons, we are motivated to propose an adaptive scheme, which employs transmit mode switching between STASM and EDAS-SM. The objective of the proposed scheme is to minimize error performance by switching between STASM and EDAS-SM, the transmission The criterion proposed for selecting the transmission mode is the ISEP. This is primarily motivated by the fact that the ISEP can be largely computed by employing a look-up-table (LUT) approach, hence limiting the CC imposed.

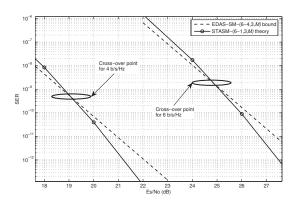


Figure 8: Cross-over points for STASM and EDAS-SM for $N_R=3$ and 4, 6 b/s/Hz.

As a note, in terms of CC (considering floating point operations (flops) [10]), the STASM scheme only requires the computation of $\|\boldsymbol{h}_j\|_F$, $j\in[1:N_T]$. This imposes $N_T(2N_R-1)$ flops only; which, is negligible compared to that of EDAS-SM [9].

4.2 System Model of the Proposed Scheme

Consider a MIMO communication system with N_T transmit antennas, N_R receive antennas and a perfect feedback link to the transmitter, as depicted in Figure 9. Transmission is based on selection between two candidate transmission modes, viz. STASM and EDAS-SM, each independently operating as discussed in Section 2. Note, as explained earlier, we consider M-QAM.

At the receiver, the corresponding detection unit is employed such as to extract the message. Furthermore, an important function at the receiver is the transmission candidate selector. In this module, based on CSIR, the candidate transmission modes are considered, such as to satisfy a target spectral efficiency defined as $\beta_{STASM} = \log_2 M$ b/s/Hz or $\beta_{EDAS-SM} = \log_2 N_{SM} M$ b/s/Hz for STASM and EDAS-SM, respectively.

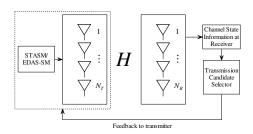


Figure 9: System model of proposed adaptive scheme.

Assuming a slowly varying channel and CSIR, the ISEP for each of the candidate transmission modes is computed, and the transmission mode is chosen such that the ISEP is minimized.

In the next two subsections, we analyze the ISEP for each of the candidate transmission modes in the proposed scheme.

4.3 ISEP for STASM

Considering M-QAM, the ISEP may be defined as:

$$P_{M_{STASM}}^{i} = 4\varphi_i - 4\varphi_i^2 \tag{21}$$

where
$$\varphi_i = \left(1 - \frac{1}{\sqrt{M}}\right) Q\left(\sqrt{\frac{3\gamma_s}{M-1}}\right)$$
 and $\gamma_s = \gamma \|\boldsymbol{h}_{\hat{j}}\|_F^2$.

4.4 ISEP for EDAS-SM

The derivation of the ISEP for EDAS-SM follows the method of [20]. On this note, the ISEP of EDAS-SM for transmit antenna $k,\ k\in[1:N_{SM}]$, can be formulated as $P_e^i(k)\geq 1-\left(1-P_a^i(k)\right)\left(1-P_b^i(k)\right)=P_a^i(k)+P_b^i(k)-P_a^i(k)\cdot P_b^i(k)$, where $P_a^i(k)$ is the ISEP of transmit antenna index error and $P_b^i(k)$ is the ISEP for M-QAM (note this is the lower bound, since we assume the probabilities $P_a^i(k)$ and $P_b^i(k)$ are independent [20]). Expressions for $P_a^i(k)$ and $P_b^i(k)$ may be derived as follows:

Given that the M-QAM transmit symbol is detected at the receiver without errors, the upper bound for $P_a^i\left(k\right)$ can be

formulated as follows [21, pp. 261-262]:

$$P_a^i(k) \le \sum_{q=1}^{M} \sum_{\hat{k}=1}^{N_T} \frac{P\left(\boldsymbol{x}_{kq} \to \boldsymbol{x}_{\hat{k}q} | \boldsymbol{H}\right)}{MN_T}$$
 (22)

where $P(x_{kq} \rightarrow x_{\hat{k}q}|H)$ is the conditional PEP of choosing $x_{\hat{k}q}$ given that x_{kq} was transmitted.

The conditional PEP can be formulated as follows:

$$P\left(\boldsymbol{x}_{kq} \to \boldsymbol{x}_{\hat{k}q} | \boldsymbol{H}\right) = P(\|\boldsymbol{y} - \boldsymbol{\alpha}_{\hat{k}}\|_{F} < \|\boldsymbol{y} - \boldsymbol{\alpha}_{k}\|_{F})$$
$$= P(\|\boldsymbol{\alpha}_{k} - \boldsymbol{\alpha}_{\hat{k}} + \boldsymbol{\eta}\|_{F} < \|\boldsymbol{\eta}\|_{F})$$
(23)

where $\alpha_k = \sqrt{\gamma} h_k s_q$ and $\alpha_{\hat{k}} = \sqrt{\gamma} h_{\hat{k}} s_q$. Employing the triangle inequality, (23) can be written as:

$$P\left(\boldsymbol{x}_{kq} \to \boldsymbol{x}_{\hat{k}q} | \boldsymbol{H} \right) = P(\|\boldsymbol{\alpha}_{k} - \boldsymbol{\alpha}_{\hat{k}}\|_{F} - \|\boldsymbol{\eta}\|_{F}) < \|\boldsymbol{\eta}\|_{F}) = P(2 \cdot \|\boldsymbol{\eta}\|_{F} > \|\boldsymbol{\alpha}_{k} - \boldsymbol{\alpha}_{\hat{k}}\|_{F}) \quad (24)$$

But $\|\eta\|_F = \sqrt{\sum_{w=1}^{N_R} (\eta_w^I)^2 + \sum_{w=1}^{N_R} (\eta_w^Q)^2}$, where the w-th element of η is given as $\eta_w = \eta_w^I + \sqrt{-1}\eta_w^Q$. As earlier, I and Q represent the in-phase and quadrature parts of a complex number.

Let
$$\bar{\eta}^2 = \min\{(\eta_1^I)^2, (\eta_2^I)^2, \cdots, (\eta_{N_R}^I)^2, (\eta_1^Q)^2, (\eta_2^Q)^2, \cdots, (\eta_{N_R}^Q)^2\}$$
; then we get:

$$P\left(\boldsymbol{x}_{kq} \to \boldsymbol{x}_{\hat{k}q} | \boldsymbol{H}\right) = P\left(2\sqrt{\sum_{w=1}^{N_R} \left(\eta_w^I\right)^2 + \sum_{w=1}^{N_R} \left(\eta_w^Q\right)^2} > 2\sqrt{2N_R\bar{\eta}^2} > \|\boldsymbol{\alpha}_k - \boldsymbol{\alpha}_{\hat{k}}\|_F\right) \quad (25)$$

Finally, with some manipulation and use of the Q-function it may be verified that (25) can be written as:

(21)
$$P\left(\boldsymbol{x}_{kq} \to \boldsymbol{x}_{\hat{k}q} | \boldsymbol{H}\right) = P\left(2\sqrt{2N_R\bar{\eta}^2} > \|\boldsymbol{\alpha}_k - \boldsymbol{\alpha}_{\hat{k}}\|_F\right)$$
$$= Q\left(\frac{\|\boldsymbol{\alpha}_k - \boldsymbol{\alpha}_{\hat{k}}\|_F}{2\sqrt{N_R}}\right)$$
(26)

where $\bar{\eta}$ is an AWGN random variable with zero mean and variance 0.5.

For M-QAM, $P_h^i(k)$ is approximately given by [14, (45)],

$$P_b^i(k) = 4\varphi_i - 4\varphi_i^2 \tag{27}$$

where
$$\varphi_i = \left(1 - \frac{1}{\sqrt{M}}\right) Q\left(\sqrt{\frac{3\gamma_s}{M-1}}\right)$$
 and $\gamma_s = \gamma \|\boldsymbol{h}_k\|_F^2$. In the next subsection, we present an example algorithm of the proposed adaptive scheme employing a target spectral efficiency of $\beta_{STASM} = \beta_{EDAS-SM} = 4$ b/s/Hz.

4.5 Example Algorithm for 4 b/s/Hz

In this subsection, an example algorithm for a target spectral efficiency of $\beta_{STASM}=\beta_{EDAS-SM}=4$ b/s/Hz is presented. The configuration of $N_T=6$ and $N_R=3$ is assumed. To satisfy the target spectral efficiency of 4 b/s/Hz, the candidate transmission modes are set as follows: a) STASM - $N_T=6,\, 16\text{-QAM},\, b)$ EDAS-SM - $N_T=6,\, N_{SM}=4,\, 4\text{-QAM}.$ The example algorithm for selection of the transmission mode proceeds as follows:

Step 1: Construct the following 3×6 matrix at the receiver:

$$\boldsymbol{H} = [\boldsymbol{h}_1 \quad \boldsymbol{h}_2 \quad \cdots \quad \boldsymbol{h}_6] \tag{28}$$

Step 2: Find $\|\mathbf{h}_{\hat{j}}\|_F^2$, such that $\|\mathbf{h}_{\hat{j}}\|_F^2 \ge \|\mathbf{h}_{j}\|_F^2$ $j \in [1:N_T], \hat{j} \neq j$.

Step 3: Compute ISEP for STASM based on (21).

Step 4: Determine all enumerations of $N_{SM}=4$ transmit antennas, where the total number of enumerations is given by $N=\binom{N_T}{N_{SM}}$.

Step 5: Determine the enumeration ℓ that maximizes the MED, such that the (i,j)-th element of D, $D_{i,j}$ for i=j is computed as:

$$D_{i,j} = 4 \cdot \|\boldsymbol{h}_i\|_F^2 \tag{29}$$

and for $i \neq j$, $D_{i,j}$ is given as:

$$D_{i,j} = \min_{s_1 \neq s_2 \in S} \| \boldsymbol{h}_i s_1 - \boldsymbol{h}_j s_2 \|_F^2$$
 (30)

$$= \min_{\substack{s_{1I}, s_{2I} \in M_1 \\ s_{1Q}, s_{2Q} \in M_2}} \|\mathbf{R} \begin{bmatrix} s_{1I} \\ s_{1Q} \\ -s_{2I} \\ -s_{2Q} \end{bmatrix}\|_F^2$$
 (31)

where \mathbf{R} is a 4×4 upper-triangular matrix having zero entries at the locations (1,2) and (3,4).

The enumeration $\ell_{selected}$ is then defined as:

$$\ell_{selected} = \underset{\ell \in [1:N]}{\operatorname{argmax}} \left(\min \boldsymbol{D}(\ell) \right) \tag{32}$$

Step 6: Compute the ISEP for EDAS-SM using (22) and (26). Hence, the overall ISEP is computed as:

$$P_{e_{Total}}^{i} = \frac{1}{4} \left(P_{e}^{i} (1) + P_{e}^{i} (2) + \dots + P_{e}^{i} (4) \right)$$
 (33)

where each $P_e^i(k)$, $k = [1, 2, \dots, N_{SM} = 4]$, takes each of the possible transmit antennas into account.

At this stage, the ISEP for STASM and EDAS-SM have been computed. Finally, the transmission mode is chosen based on the minimum ISEP and the transmitter is notified of the chosen mode via the feedback link (refer to Figure 9).

4.6 Analysis of CC

In this subsection, the CC of the proposed adaptive transmit mode switching scheme is analyzed in terms of flops, similar to [10].

Steps 1 and 4 do not impose any flops. Step 2 involves $2(N_R-1)N_T$ flops. In Step 3, $\|\boldsymbol{h}_{\hat{j}}\|_F^2$ has already been computed. Hence, only 5 flops are required and a LUT can be used for computation of the Q-function and square-root operations. Step 5 involves the selection of the enumeration of N_{SM} transmit antennas and since $\|\boldsymbol{h}_j\|_F^2$, $j \in [1:N_T]$, has been already computed, imposes only $64\binom{N_T}{2}(N_R-\frac{2}{3})\frac{M}{4}$ flops [9]. Finally, Step 6 may also employ the LUT for computation of the Q-function and square-root operations. Hence, it may be validated that $N_{SM}(11+3N_R)-2$ flops are imposed. Therefore, the overall imposed CC is given by $\delta_{adaptive}=2(N_R-1)N_T+64\binom{N_T}{2}(N_R-\frac{2}{3})\frac{M}{4}+N_{SM}(3N_R+11)+3$ flops.

4.7 Numerical Results

In this subsection, we evaluate the average SER versus SNR for the proposed adaptive system and draw comparison between the CC for the adaptive scheme and its closed-loop counterparts, i.e. EDAS-SM and STASM. We consider a Rayleigh frequency-flat fading channel and complete knowledge thereof at the receiver. The Monte Carlo simulation results for a spectral efficiencies of 4 b/s/Hz and 6 b/s/Hz are presented in Figures 10 and 11, respectively, for $N_R = 1$, 2 and 3. In the case of 4 b/s/Hz, for $N_R = 1$, the error performance of the proposed system matches STASM, which was superior across the SNR range. For $N_R = 2$, up until 10 dB, the SER of both EDAS-SM and STASM are identical, after which the cross-over point manifests and STASM is superior. The proposed scheme follows STASM in this region of SNRs. The proposed scheme completely follows EDAS-SM for $N_R=3$.

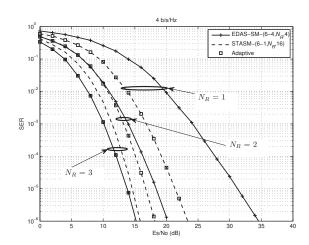


Figure 10: Comparison of SER performance for STASM, EDAS-SM and the proposed adaptive scheme for different N_R and 4 b/s/Hz.

For a spectral efficiency of 6 b/s/Hz, identical behavior is demonstrated (refer to Figure 11) for $N_R=1$. Considering $N_R=2$, which clearly shows how STASM outperforms EDAS-SM after the cross-over point, it is demonstrated

that the proposed adaptive system follows the minimum error performance curve of STASM/EDAS-SM. In the case of $N_R=3$, the proposed adaptive scheme completely follows EDAS-SM. Hence, the proposed scheme exploits the advantages of both EDAS-SM and STASM, such as to improve reliability.

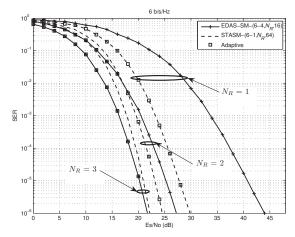


Figure 11: Comparison of SER performance for STASM, EDAS-SM and the proposed adaptive scheme for different $N_{\rm R}$ and 6 b/s/Hz.

Table 1 tabulates the CC for the adaptive scheme compared to EDAS-SM and STASM. We consider 4 b/s/Hz and 6 b/s/Hz, similar to Figure 10 and 11. The CC of EDAS-SM is given in [10, Section III.B]. As expected, it is evident that the adaptive scheme imposes a slightly larger CC compared to EDAS-SM and is at worst-case 16% larger for $N_R=1$, while providing an SNR gain of more than 10 dB. For $N_R=2$ and $N_R=3$, the worst-case increase is 5%.

Table 1: Comparison of CC.

Scheme	Spectral efficiency	No. of flops
EDAS-SM	4 b/s/Hz	$326(N_R = 1), 1, 298(N_R = 2), 2, 270(N_R = 3)$
STASM	4 b/s/Hz	$6(N_R = 1), 18(N_R = 2), 30(N_R = 3)$
Adaptive	4 b/s/Hz	$379(N_R = 1), 1, 363(N_R = 2), 2, 347(N_R = 3)$
EDAS-SM	6 b/s/Hz	$1,286(N_R=1), 5,138(N_R=2), 8,990(N_R=3)$
STASM	6 b/s/Hz	$6(N_R = 1), 18(N_R = 2), 30(N_R = 3)$
Adaptive	6 b/s/Hz	$1,339(N_R=1),5,203(N_R=2),9,067(N_R=3)$

5. CONCLUSION

In this paper, closed-form expressions for the ASEP of STASM with M-QAM and M-PSK were presented. The formulated ASEP expressions were relatively easy to evaluate and further validated the Monte Carlo simulation results. Comparisons have been drawn with EDAS-SM. STASM achieves full-diversity compared to EDAS-SM; however, the cross-over point may occur in the moderate-to-high SNR region. Hence, an adaptive system with two candidate transmission modes (STASM/EDAS-SM) was proposed and investigated; the error performance was minimized across the SNR range.

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