A mathematical mould model for transient infiltration and lubrication behaviour of slag in a steel continuous casting process

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Synopsis

The transient infiltration and lubrication behaviour of slag during continuous casting of steel is important for billet quality. A two-dimensional coupled mathematical mould model was developed to investigate these phenomena. The accuracy of the model was verified by comparing the calculated slag consumption with measurements by the plant. The results show that the liquid slag is consumed from the middle and late period of positive strip time to the next early period of positive strip time, including the entire negative strip time. The maximum downward infiltration velocity and positive pressure in the slag channel is at the middle of the negative strip time. Increasing the positive pressure of the slag channel is conducive to lubrication. The shear stresses acting on the shell surface and at the mould side were determined by the lubrication slag consumption and total slag consumption, respectively, and gradually decreased with increasing slag consumption. The negative strip time was lengthened to increase the slag consumption and prolong the time near the maximum downward shear stress, so as to be conducive to the demould.

Keywords

lubrication, slag consumption, slag infiltration, shear stress, continuous casting.

Introduction

Most of the world’s steel is produced by the continuous casting process, in which molten steel is continuously injected into a water-cooled mould. The molten steel solidifies along the mould wall, and the semi-finished billet is continuously pulled from the lower part of the mould (Youming, Yeming, and Kuangdi, 2022). Billets with diverse sizes, shapes, and qualities are produced. Continuous casting has the advantages of high quality products and cost efficiency (Louhenkilpi, 2014).

The slag plays an important role in continuous casting by providing effective heat insulation (Yang et al., 2020) and lubrication (Zhang et al., 2018; Yan et al., 2019), preventing secondary oxidation of molten steel and improving heat transfer within the mould. Liquid slag infiltrates from the slag pool into the gap between the shell and mould wall, forming a slag film that is conducive to lubrication and prevents the shell from sticking to the mould wall.

The behaviour of slag in the continuous casting process has been the subject of numerous studies. A semi-empirical model was proposed by Shin et al. (2006) to predict slag consumption based on plant measurements, but a description of transient slag consumption was omitted. The phenomenon of slag infiltration and initial shell solidification in the meniscus was characterized though an integrated model (Ramirez-Lopez et al., 2010; Ramirez-Lopez, Lee, and Mills, 2010). The total slag consumption near the meniscus was calculated, but the result was slightly higher than that shown from plant data. Jonayat and Thomas (2014) studied the effects of casting parameters on slag consumption by a computational model of the meniscus region; however, the meniscus shape was prefixed and the solidified shell was not considered. Yang, Meng and Zhu (2014, 2018) described the transient pressure variation of liquid slag in the channel using a cold model, and analysed the impact of casting speed on liquid slag consumption by means of a two-dimensional coupling model. The impact of the modification ratio (α) of non-sinusoidal oscillation on slag lubrication was investigated by Yan et al., (2019) but the model only took into account the liquid slag consumption. Zhang et al. (2019a, 2019b, 2021) investigated the infiltration of slag, and compared the effects of different casting parameters on total slag consumption. Slag infiltration at the corner of the mould was described by Ji et al. (2023) through a three-dimensional mathematical model. However, there was little information considered regarding the evolution of lubrication consumption of liquid slag and friction. Understanding the infiltration and lubrication behaviour of slag was found conducive to smoothly demolding of the shell from the mould and improving lubrication between the slab and the mould.
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In the current work we established a coupled model to investigate the transient infiltration and lubrication behaviour of slag. The accuracy of the model was verified by comparing the calculated slag consumption with measurements by the plant. The transient variation in infiltration velocity of slag in the slag channel, pressure in the slag channel, thickness of the liquid and solid slag layers, shell surface temperature, heat flux of the copper plate, total slag consumption, lubrication consumption, the shear stress of the liquid slag on the shell surface, and shear stress at the mould wall were monitored at 300 mm below the meniscus. The transient infiltration of slag and slag lubrication were analysed, providing a theoretical basis for controlling the slag consumption and shear stress, thereby enhancing the lubrication effect of the slag and improving the surface quality of billets.

Description

Assumptions

The assumptions were proposed based on describing the industrial production of continuous cast slab through numerical simulation calculation:

➤ Due to the symmetry of the flow and temperature fields in the mould, half of the mould was used as the calculation domain.
➤ Molten steel is an incompressible Newtonian fluid.
➤ The impact of mould taper on flow and heat transfer were not taken into consideration, and the dimensional change of casting slabs caused by solidification cooling shrinkage was ignored.
➤ The solid-liquid phase was considered a porous medium during solidification.

Model description

The mould model included the submerged entry nozzle (SEN), copper plate, and fluid domain (steel-slag-air), as shown in Figure 1a. The steel surface was covered with slag and air, each with a thickness of 50 mm. ICEM was used to build the mesh. The total amount of mesh elements was 168 962, and the area near the fluid-solid interface was subjected to mesh refinement with a minimum mesh size of 50 μm (Figure 1b).

Fluid flow, heat transfer, and solidification during the continuous casting process were included in the model. ANSYS Fluent 19.2 was employed to solve the Navier-Stokes equations. The volume of fluid method (VOF) was used to calculate the phase fractions. The interface was tracked by continuous surface forces (CFS). The k-ε model was utilized to solve turbulent flow. The solidification of fluid was solved by using the solidification model.

The boundary settings are shown in Figure 2. The boundary of the upper surface was set as a free surface with a temperature of 300 K. The boundary of the mould outlet was set to outflow, resulting in a fully developed flow at this boundary. The interface between the fluid and solid was defined as a coupled wall, the fluid-mould interface was coupled in terms of velocity and heat flux, and oscillated with the mould. The walls of the SEN and top and bottom walls of the mould were set as insulated due to the negligible heat flux across these walls in the real process. A symmetric boundary condition was applied for the plane of symmetry. The boundary of the SEN inlet was set to velocity inlet, where the inlet velocity \( V_{in} \) was determined by the mass balance as shown in Equation [1], and the inlet temperature was 1830 K. The cold wall of the copper plate was set as a convection boundary with the water temperature 305 K and the heat transfer coefficient \( h_c \) as per the empirical determination by Xiang, Xia, and Wu (2023) of 28 000 W/m²K, correlating to a water flow rate of 10 m/s. Similarly, the wall of the secondary cooling zone was set as a convection boundary with the water spray temperature 300 K and heat transfer coefficient \( h_s \) 2000 W/m²K correlating to a specific water flow in the secondary cooling zone of 1.03 L/kg as determined by Zang et al. (2019). The oscillation mode of the mould was sinusoidal. The velocity and displacement expressions of mould oscillation are illustrated in Equations [1]–[5]. A dynamic mesh was employed to achieve the oscillation of the mould.

\[
V_{in} = \frac{A_{in} \times V_c}{A_{in}} \tag{1}
\]

where \( V_c \) is the casting speed (m/min), \( A_{in} \) the inlet area (m²), and \( A_{out} \) the outlet area (m²).

\[
V_m = \frac{4Mhf\varepsilon \cos(2\arctan[M\tan(\pi f/\omega)])}{1 + M^2 + (1 - M^2) \cos(2\pi f/\omega)} \tag{2}
\]

\[
M = \cot \left( \frac{\pi}{4} \right) \left( 1 + \alpha \right) \tag{3}
\]

where \( V_m \) is the mould velocity (m/s), \( h \) the oscillation amplitude of the mould (m), \( f \) the oscillation frequency (Hz), \( \alpha \) the modification ratio (sinusoidal mode when \( \alpha \) was zero), and \( S_m \) mould displacement (m).

Figure 1—(a) Schemes of model, (b) mesh

Figure 2—Boundary of the model
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The break temperature of the slag was utilized to distinguish the liquid and solid phases since the formation of the first solids in the liquid slag is related to the break temperature (Kölbl and Harmuth, 2019). The time step of the solution was 0.0001 seconds, and the results were calculated for more than a month of casting. The detailed governing equation, casting parameters, model parameters, and material properties are described elsewhere (Cao et al., 2023).

Validation of slag consumption

The model was validated in Cao et al. (2023) by comparing the oscillation marks with plant measurements and the pitch of oscillation marks with the theoretical values, respectively. In addition, the 17 cases in Table I were simulated, and the slag consumption was calculated during one cycle after the calculation was stable. The slag consumptions were compared with the plant measurements (Shin et al., 2006). Figure 3a shows that the calculated slag consumption was in good agreement with the plant measurements. The slag consumption decreased with increasing casting speed (Figure 3b), which is consistent with observations by Shin et al. (2006)

Based on the above, the depth of the oscillation mark and the slag consumption were compared with the plant measurements. The two-dimensional model showed good accuracy and robustness, and hence could be used to study the lubrication behaviour of slag.

Results and discussion

Under the mould oscillation for \( f = 174 \text{ cpm}, \ h = 2.9 \text{ mm}, \ a = 0 \) with \( V_t = 1.4 \text{ m/min} \), the specific variables at 300 mm below the meniscus were tracked to investigate the transient infiltration of slag and slag lubrication. The velocity and displacement of mould oscillation are presented in Figure 4, where the time period when the downward oscillation velocity exceeds the pulling speed is negative strip time \( (t_n) \), and the rest period the positive strip time \( (t_p) \).

<table>
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<td>Operating conditions and calculated slag consumption</td>
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![Figure 3](image)

Figure 3—(a) Validation of predicted slag consumption per oscillation cycle with measurements taken at different positive strip times, (b) effect of casting speed on slag consumption in each oscillation cycle.
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Infiltration velocity of slag and pressure in slag channel

The transient downward infiltration velocity of slag in the slag channel is shown in Figure 5. During the early and late stages of \( t_p \), the slag flowed upward owing to the upward oscillation of the mould. During the \( t_m \), the downward infiltration of the slag was accelerated due to the increase in the downward oscillation velocity of the mould, reaching a maximum of 0.032 m/s at the middle stage, followed by a gradual decrease in infiltration velocity. The infiltration velocity of slag was determined by the velocity and position of mould oscillation.

The variation of the pressure in the slag channel in a cycle is illustrated in Figure 6. The pressure varied between the maximum positive and negative pressures. The slag channel experienced negative pressure during the early and late stages of \( t_p \) with a maximum value of 12 167.55 Pa. However, the slag channel experienced positive pressure during the \( t_m \) reaching a maximum value of 24 671.961 Pa at the middle of the \( t_m \). The pressure in the slag passage was affected by mould oscillation and the movement of the slag rim (Cao et al., 2023).

The variation of slag pressure exerted an influence on the meniscus and the initial shell, resulting in periodic deformations (i.e. oscillation marks). Increasing the negative pressure of the slag channel was conducive to enhancing the effect of liquid slag infiltration in the slag channel, and improving the lubrication effect. Increasing the positive pressure of the slag channel was conducive to forced demoulding and preventing breakout. However, an increase in both maximum positive and negative pressures resulted in an increasing pressure difference within the slag channel, exacerbating meniscus fluctuations and initial shell deformations, which is not conducive to improving the surface quality of slabs. Therefore, it was crucial to control these parameters.

Thickness of slag film

The surface temperature of the shell and heat flux of the copper plate are shown in Figure 7. The heat flux was within 1.83 to 3.44 MW/m², and the surface temperature of the shell was within the range 1487.20 to 1524.13 K. The maximum temperature and minimum heat flux appeared near the \( t_n \). The higher the surface temperature of the shell, the faster the slag melting rate, resulting in a thicker liquid slag layer, which is conducive to lubrication. The greater the heat flux, the thicker the solid slag layer, which is not conducive to the solidification of liquid steel into a shell.

The transient variation in thickness of solid and liquid slag layers is exhibited in Figure 8. The thickness variation of the solid slag layer was inversely related to that of the liquid slag layer, and the thicknesses were 1.31 to 1.37 mm and 0.19 to 0.28 mm, respectively. At the middle of the \( t_m \), the liquid layer affected by fast flowing slag became thinner and the solid layer became thicker. The maintenance of a thick and uniform liquid slag film, while ensuring a thin solid slag film, was crucial in order to prevent breakout.

Slag consumption

The slag film could prevent the shell sticking to the mould wall, which contained the liquid and solid layers. The liquid slag layer could help the shell to demould smoothly. The slag consumption was an important index for evaluating the lubrication performance of the slag. The slag consumed in the total slag film was considered as total slag consumption \( (Q_t, \text{kg/s}) \), while the slag consumed in the liquid slag film was considered as lubrication consumption.
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(Qub, kg/s). Transient lubrication consumption and total slag consumption are presented in Figure 9, where the minus sign indicates upward movement of slag.

The slag consumption tended to increase during the t, The variation of Q and Qub was similar, with average values of 0.03 and 0.009 kg/s, respectively. The liquid slag was pumped into the slag channel under positive pressure. The maximum Q and Qub were observed near the middle of t, with values of 0.118 and 0.011 kg/s, respectively.

The mechanism of liquid slag consumption was elucidated according to the above slag consumption, the flow and pressure of slag in the slag channel, and the variation of slag film thickness. The liquid slag flowed upward due to the upward movement of the mould during the early stage of t; the inertial effect weakened and the lubrication consumption increased with the decrease in upward oscillation velocity of the mould. As the upward velocity of the mould decreased to zero and the mould began to oscillate downward, the downward flow of liquid slag was facilitated by the inertial effect of the mould and liquid slag continued to be consumed, reaching the maximum value of 0.0115 kg/s at the initial stage of t. After that, although the liquid slag infiltrated into the slag channel under the action of the increased positive pressure and slag infiltration velocity, the decrease in thickness of the liquid slag film led to a decrease in lubrication consumption. The lubrication consumption decreased to 0.0111 kg/s at the middle of t. Later, the lubrication consumption began to increase with the increase in thickness of the liquid slag film. With the upward oscillation of the mould, the slag consumption decreased due to the weakening of the suction and the inertial effect of the mould. The lubrication consumption was minimum at -0.0061 kg/s at the end of t. Liquid slag was consumed from the middle and late period of t to the next early period of t, including the entire t.

Shear stress

Shear stress acting on the shell surface (τs/l) and at the mould side (τmold), Pa were important parameters which characterized the slag lubrication and the interaction between the mould wall and shell, and the surface quality of the shell and productivity of continuous casting were directly affected. Hence, τs/l and τmold were calculated according to Equations [4] and [5] (Meng and Thomas, 2003), respectively:

\[
\tau_{s/l} = \mu_{s/l} \frac{\partial y_{y}}{\partial \alpha}
\]

\[
\tau_{mold} = - \int_{x=0}^{a} \frac{d\sigma_{y}}{d\alpha} \cdot dx + \tau_{s/l} = \frac{\nu}{1-\nu} \rho_{steel} G d_s + \tau_{s/l}
\]

where: \(\mu_{s/l}\) is the viscosity of the slag(Pa-s), \(V_y\) is the vertical velocity of the slag (m/s), \(a\) the thickness of the liquid slag layer, \(\alpha\) the axial stress in the solid slag layer, \(d\) the thickness of the solid slag layer (mm), and \(\nu\) the Poisson’s ratio of the slag (0.17 in the current study).

The upward shear stress on the shell surface (τs/l) and shear stress at the mould side (τmold) are plotted in Figure 10. The variations in τs/l and τmold were inversely related to the variations in Qub and Q, respectively. The τs/l was within 29.62 to 209.75 Pa, τmold was within 18.35 to 19.54 kPa, and the maximum occurred when the mould was near the equilibrium position during the t. During the t, the τs/l decreased with the increase in slag consumption, reaching the minimum at the middle of t, and subsequently increased with a decrease in slag consumption. The τmold fluctuated around the minimum value of 18.55 kPa due to the fluctuation in lubrication slag consumption. The shear stress depended on the velocity gradient of the slag, slag viscosity, and the thickness of the solid and liquid slag films. Adequate slag consumption could reduce shear stress, avoid breakout, and be conductive to demould.

Conclusions

A two-dimensional coupled mathematical model was employed to study the infiltration and lubrication behaviour of the slag during continuous casting of steel. The infiltration velocity of slag and the pressure in the slag channel, the thickness of the liquid and solid slag layers, the total slag consumption, the lubrication slag consumption, and the shear stress of the liquid slag on the shell surface and at the mould wall were investigated. The conclusions can be summarized as follows.

- The mould oscillation led to periodic variations in the pressure and infiltration velocity in the slag channel. During the early and late stages of positive strip time (t), the slag flowed upward and the slag channel pressure was maximum negative pressure. At the middle of the negative strip time (t), infiltration velocity and the slag channel pressure reached maximum downward infiltration velocity and maximum positive pressure, respectively.

- The thickness variation of the solid slag layer was inversely related to that of the liquid slag layer, and was determined by the cooling strength and surface temperature of the shell. At the middle of the t, the thickness of the liquid layer with fast flowing slag became thinner and the solid layer became thicker.

- The variations of Qub and Q were similar. Slag consumption tended to increase during the t, and the peak values for Qf

Figure 9—Total slag consumption, lubrication slag consumption, and average slag consumption during the t and t

Figure 10—Upward shear stress of the liquid slag on the surface of the shell and shear stress at the mould side
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and $Q_{sh}$ were observed near the middle of $t_m$. The liquid slag was consumed from the middle and late period of $t_f$ to the next early period of $t_p$ including the entire $t_n$. The $t_{cf}$ and $t_{mould}$ were determined by $Q_{sh}$ and $Q_s$ respectively, and gradually decreased with increasing slag consumption. The maximum $t_{cf}$ and $t_{mould}$ occurred when the mould was near the equilibrium position during the $t_p$. The minimum $t_{cf}$ and $t_{mould}$ occurred during the $t_n$.

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Conflicts of Interest: The authors declare that they have no conflict of interest.

Data availability: The data that supports the findings of this study is available on request from the corresponding author.

References


